

1. Optimization problem for designing the stiffest bar for a given volume can be written as :

$$\text{Min}_{A(x)} SE = \int_0^L \frac{1}{2} EAu'^2 dx$$

Subject to

$$\lambda : (EAu')' + p = 0$$

$$\Lambda : \int_0^L A dx \leq V^*$$

Select the adjoint equation for the above problem.

- a)  $(EA\lambda')' = -(EAu')'$
  - b)  $(EA\lambda')' = (EAu')'$
  - c)  $(EA\lambda')' = pu$
  - d)  $(EA\lambda')' = -pu$
2. For constant axial load throughout the length of the bar, the area profile of a stiffest bar for a given volume...
- a) varies as the cube of x along the x-axis
  - b) varies as the square of x along the x-axis
  - c) varies linearly along the x-axis
  - d) is uniform along the x-axis
3. Which of the following statements about area profile of a stiffest bar for a given volume is false?
- a) Lagrange multiplier function corresponding to the equilibrium equation is equal to axial deformation.
  - b) Optimal area profile is independent of the load.
  - c) Axial strain in the bar is a constant throughout the bar.
  - d) The bar is uniformly stressed.
4. Solve the problem with  $J = \int_0^L p u dx$  minimized instead of  $SE = \int_0^L \frac{1}{2} EAu'^2 dx$  in the optimization problem to find the stiffest bar for a given volume. Which of the following change(s)?
- a) Only the design equation.
  - b) Only the adjoint equation.

- c) Both design and adjoint equations.
- d) None of the above.

5. Which of the following mathematical concepts would you need to arrive at Euler-Lagrange equations for a functional with three independent variables ?

- a) Divergence theorem
- b) Fundamental lemma of calculus of variations
- c) First variation of a functional at optimum should be zero
- d) All of the above

6. Which of the following represents Euler-Lagrange equation for  $F(z, z_x, z_y)$  ?

- a)  $\frac{\partial F}{\partial z} - \frac{d}{dx} \left( \frac{\partial F}{\partial z_x} \right) = 0$
- b)  $\frac{\partial F}{\partial z} - \frac{d}{dy} \left( \frac{\partial F}{\partial z_y} \right) = 0$
- c)  $\frac{\partial F}{\partial z} + \frac{d}{dx} \left( \frac{\partial F}{\partial z_x} \right) = 0$
- d)  $\frac{\partial F}{\partial z} + \frac{d}{dy} \left( \frac{\partial F}{\partial z_y} \right) = 0$
- e)  $\frac{\partial F}{\partial z} - \frac{d}{dy} \left( \frac{\partial F}{\partial z_x} \right) - \frac{d}{dx} \left( \frac{\partial F}{\partial z_y} \right) = 0$
- f)  $\frac{\partial F}{\partial z} - \frac{d}{dx} \left( \frac{\partial F}{\partial z_x} \right) - \frac{d}{dy} \left( \frac{\partial F}{\partial z_y} \right) = 0$

7. Identify the equation obtained by minimizing

$$\int \left\{ \frac{1}{2} \left[ \left( \frac{\partial \phi(x, y)}{\partial x} \right)^2 + \left( \frac{\partial \phi(x, y)}{\partial y} \right)^2 \right] + f(x, y) \phi(x, y) \right\} dx dy = 0 .$$

- a) Laplace's Equation in 2D
- b) Poisson's Equation in 2D
- c) Laplace's Equation in 3D
- d) Poisson's Equation in 2D

Study the Matlab code provided, BarOpt2.m, and answer questions from 8-10.

8. Identify the boundary condition corresponding to the Matlab variables:

`dispID=[n+1];`

`dispVal=[0];`

- a) free-fixed
- b) fixed-fixed
- c) free-free
- d) fixed-free

9. Which of the following Matlab script definition gives a uniform distributed force ?

- a. `F = 10*ones(n+1,1)`
- b. `F(n/2,1)=50;`
- c. `F(n+1,1)=100;`
- d. `F(1,1)=100;`

10. How did we compute first derivative of the axial displacement while implementing optimality criteria code in Matlab?

- a) Analytically; from the governing equation of the bar.
- b) Analytically; from the design equation of the stiffest bar.
- c) Numerically; using forward-difference.
- d) Numerically; using central-difference.